



ПРО ВІДХИЛЕННЯ ШВИДКИХ ЗАРЯДЖЕНИХ ЧАСТИНОК ЗІГНУТИМИ КРИСТАЛАМИ

І.В. Кириллін, М.Ф. Шульга

ІТФ ім. О.І. Ахієзера, ННЦ ХФТІ

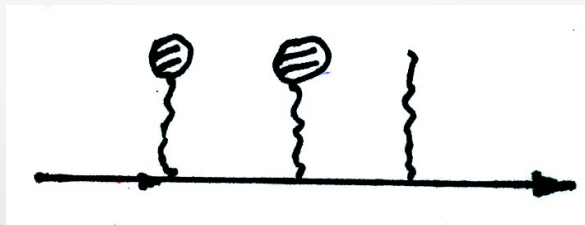
Семінар, присвячений пам'яті *Петра Івановича Фоміна*
«КВАНТОВА ТЕОРІЯ ПОЛЯ ТА КОСМОЛОГІЯ»

5 липня 2022 р.

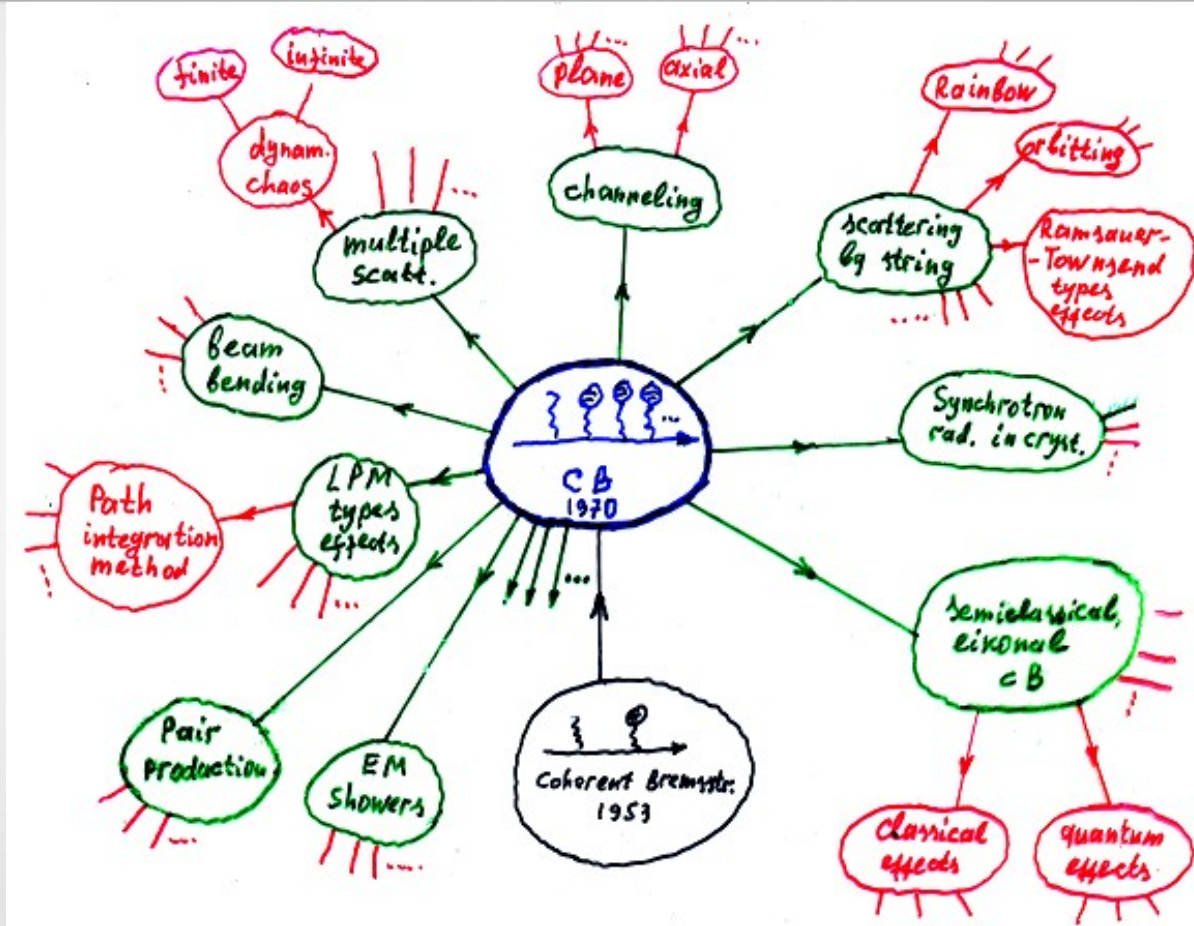
А.И. Ахиезер, П.И. Фомин, Н.Ф. Шульга

Когерентное тормозное излучение электронов и
позитронов ультрарелятивистской энергии в
кристаллах

Письма ЖЭТФ, 1971, Т. 13, с. 713-715



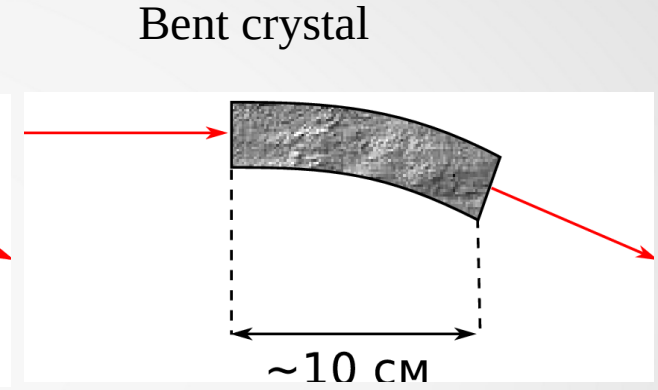
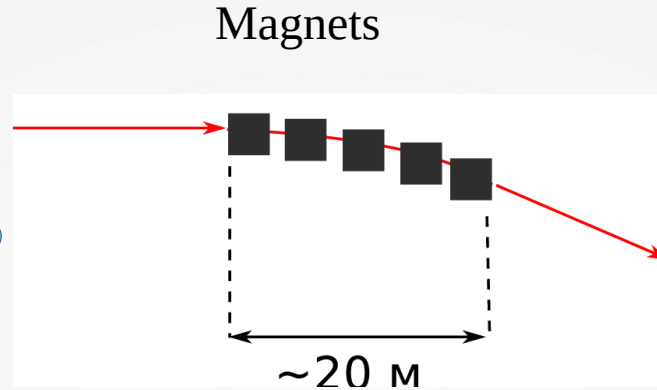
Проблемы, порожденные теорией когерентного излучения в кристаллах



Bent crystals and magnetic deflection systems

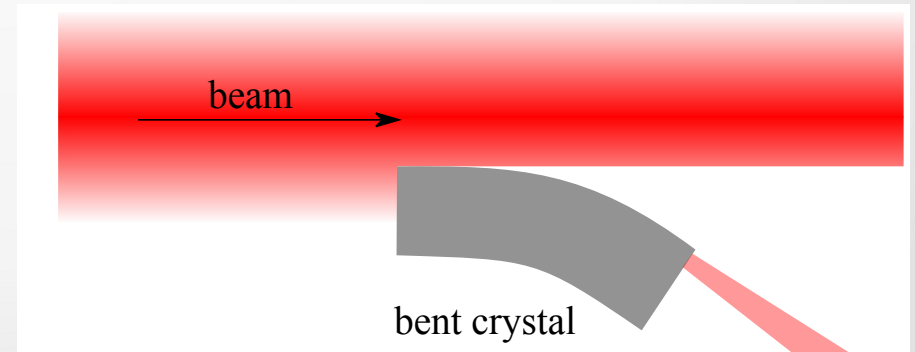


$$E_{\text{str}} \sim 10^{10} \text{ V/cm}$$
$$E_{\text{pl}} \sim 10^9 \text{ V/cm}$$



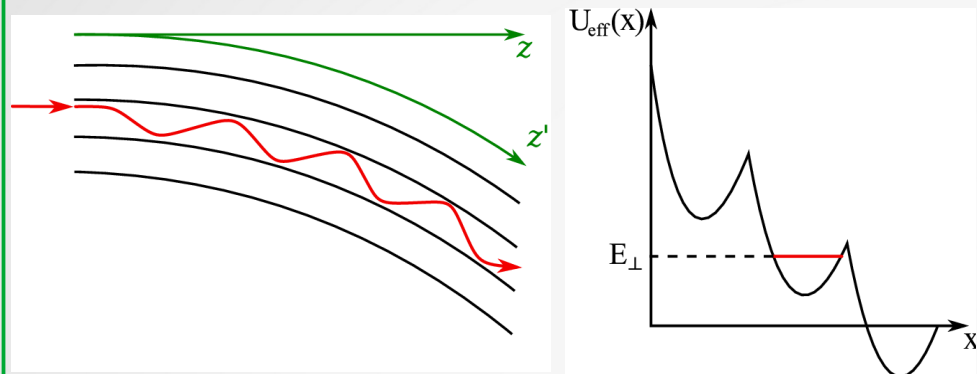
Advantages of bent crystals in comparison with magnetic deflection systems:

- Small size
- do not need electricity consumption
- do not need cooling

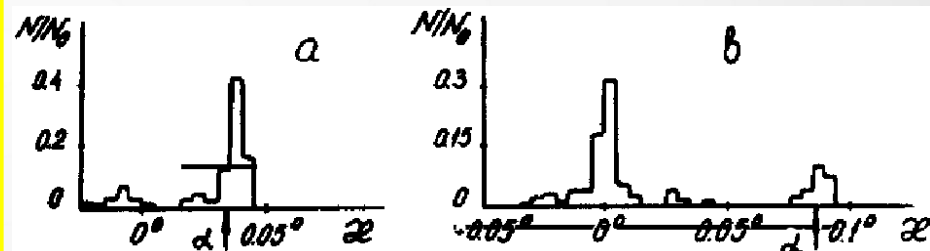


Planar channeling

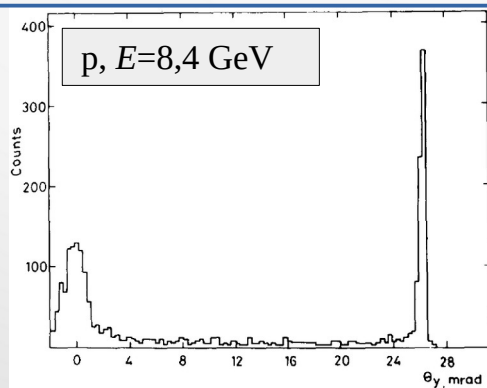
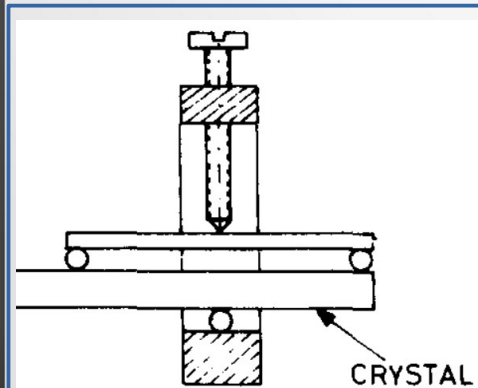
Tsyganov E. N. Fermilab TM-682, TM-684. 1976.



Таратин А. М., Цыганов Э. Н., Воробьев С. А. Поворот пучков заряженных частиц изогнутым монокристаллом. Численный эксперимент. Письма в ЖТФ. 1978. Т. 4. С. 947–950.
 Tarantin A. M., Tsyganov E. N., Vorobiev S. A. Computer simulation of deflection effects for relativistic charged particles in a curved crystal. Phys.Lett. A. 1979. Vol. 72, No. 2. P. 145–146.



p, E=1 GeV, a) R=0,29 cm, b) R=0,112 cm



Elishev A. F., Filatova N. A., Golovatyuk V. M. et al. (I.A. Grishaev, G.D. Kovalenko, B.I. Shramenko) Steering of charged particle trajectories by a bent crystal. Phys. Lett. B. 1979. Vol. 88, No. 3-4. P. 387–391.

Volume reflection

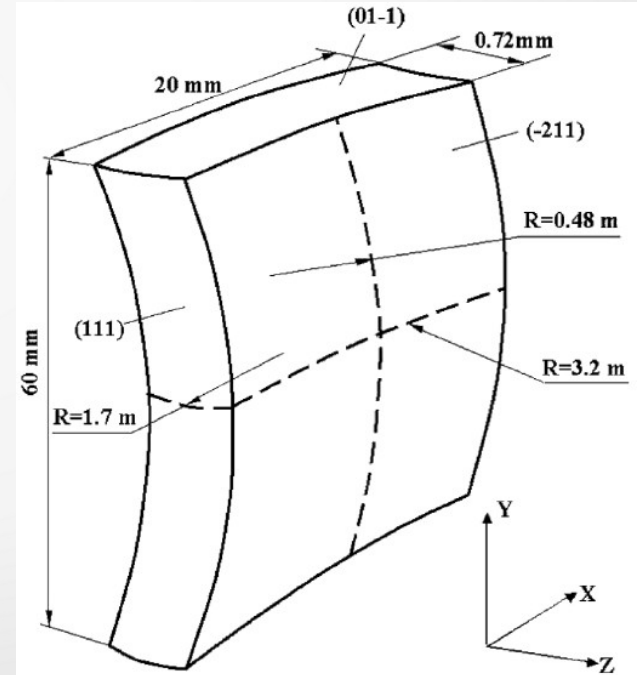
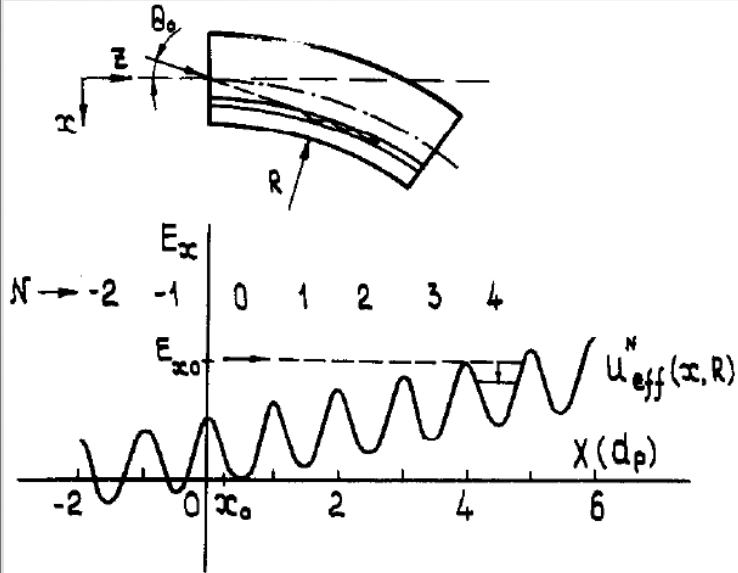
Taratin A. M., Vorobiev S. A. *Phys. Lett. A*. 1986. Vol. 115, No. 8. P. 398–400.

Taratin A. M., Vorobiev S. A. *Nucl. Instrum. Meth. B*. 1987. Vol. 26, No. 4. P. 512–521.

Taratin A. M., Vorobiev S. A. *Phys. Lett. A*. 1987. Vol. 119, No. 8. P. 425–428.

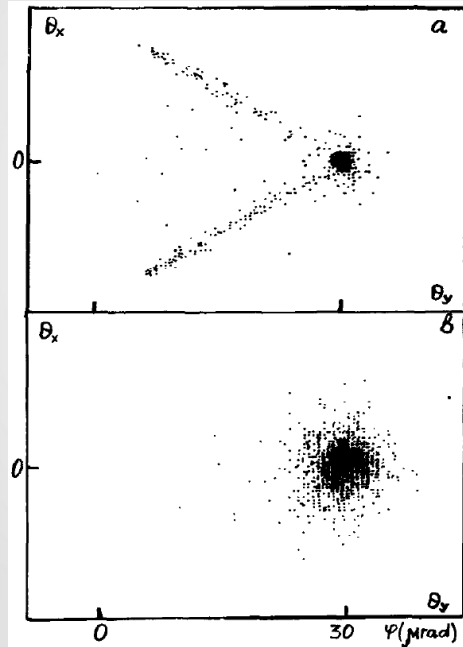
$$E_x = \frac{pv\theta_x^2}{2} + U_{eff}(x, R)$$

$$U_{eff}(x, R) = U(x) + pv\frac{x}{R}$$



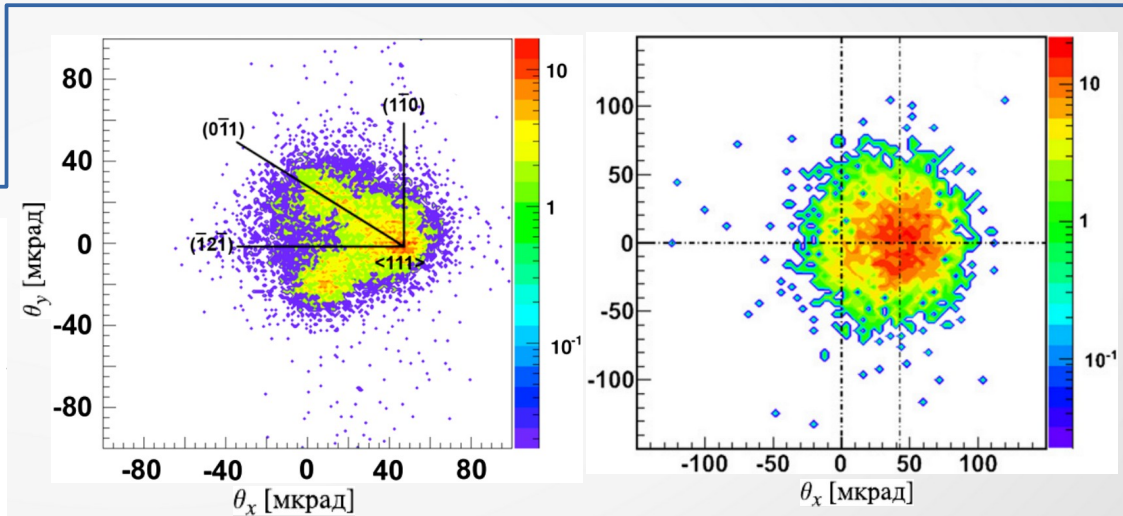
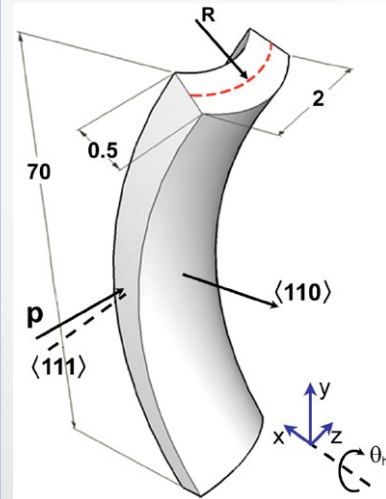
Stochastic deflection

Grinenko A. A., Shul'ga N. F. *J. Exp. Theor. Phys. Lett.* 1991. Vol. 54. P. 524–528.
 Greenenko A. A., Shul'ga N. F. *Nucl. Instrum. Meth. B.* 1994. Vol. 90, No. 1-4. P. 179–182.
 Shul'ga N. F., Greenenko A. A. *Phys. Lett. B.* 1995. Vol. 353, No. 2. P. 373–377.



$E=10$ TeV

$$\langle \psi^2 \rangle = \frac{lL}{R^2} \leq \psi_c^2$$



Scandale W., Vomiero A., Baricordi S. et al. *High-efficiency deflection of high-energy protons through axial channeling in a bent crystal.* *Phys. Rev. Lett.* 2008. Vol. 101, No. 16. P. 164801.

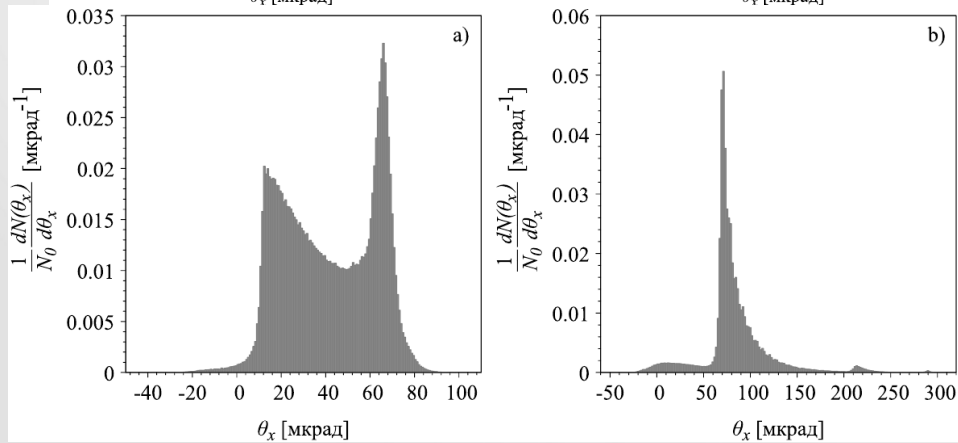
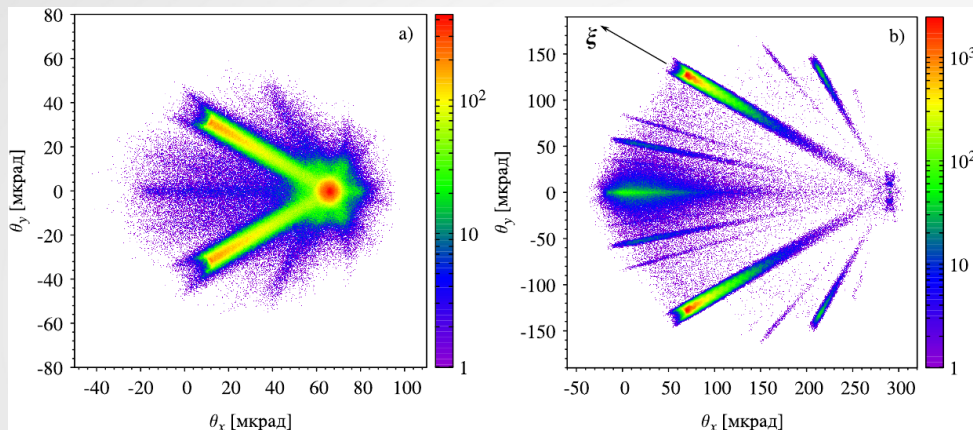
Scandale W., Vomiero A., Bagli E. et al. *High-efficiency deflection of high-energy negative particles through axial channeling in a bent crystal.* *Phys. Lett. B.* 2009. Vol. 680, No. 4. P. 301–304.

Changing the shape of the beam

R=30,3 m

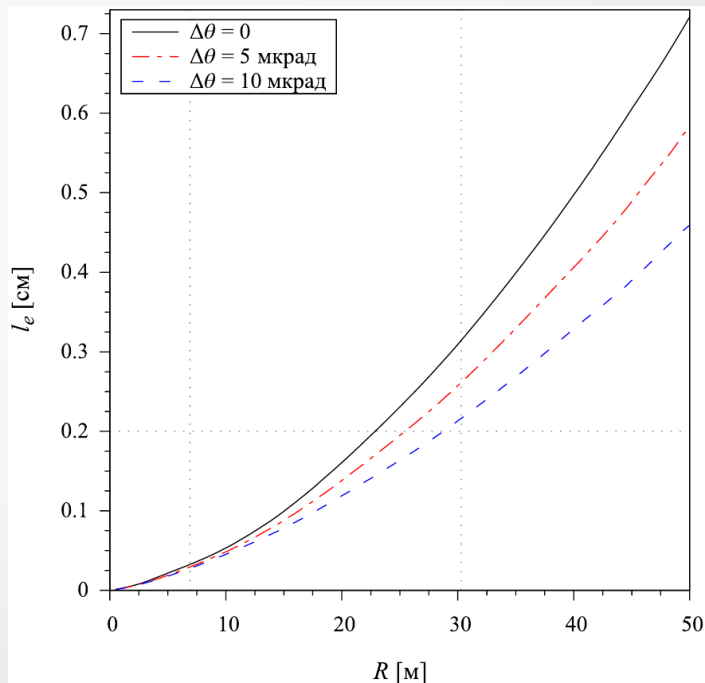
R=6,9 m

$p, E=400 \text{ GeV}, \text{Si } \langle 111 \rangle, L=2 \text{ mm}$



$$|\varphi_{pl}| = \pi/6 \rightarrow R_{cr} \approx 35 \text{ cm}$$

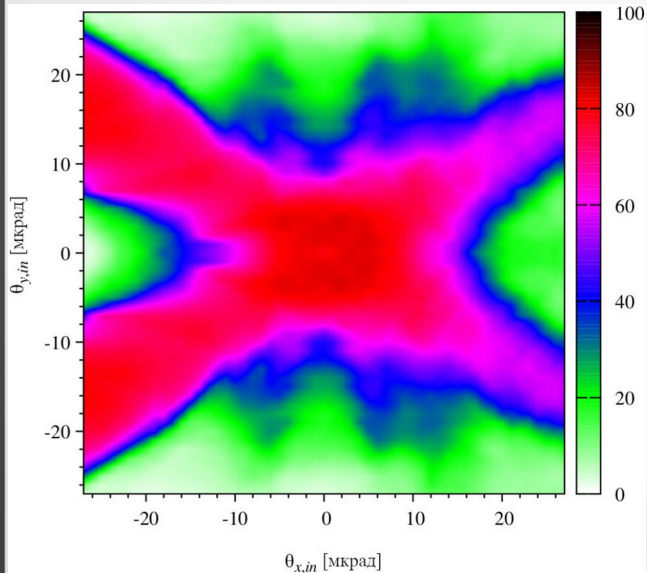
$$\frac{dN}{dl} = -CN \rightarrow N_{pl}(l) = N_0 \left(1 - e^{-l/l_e}\right)$$



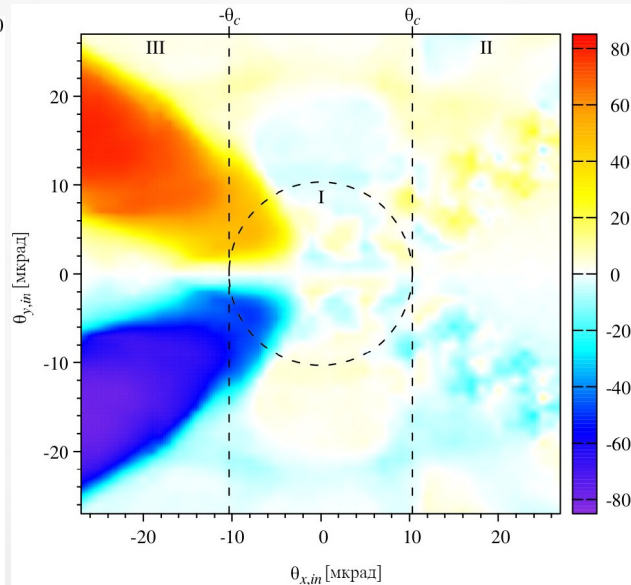
Changing the shape of the beam

$p, E=400 \text{ GeV, Si } \langle 111 \rangle, L=2 \text{ mm, } R=6,9 \text{ m}$

$$\frac{N_{(0\bar{1}1)} + N_{(\bar{1}01)}}{N_0}$$

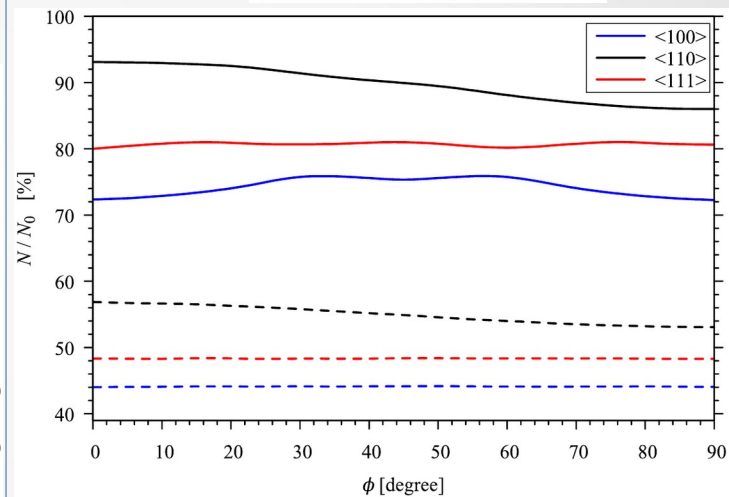


$$\frac{N_{(0\bar{1}1)} - N_{(\bar{1}01)}}{N_0}$$



$$\alpha_{st} = \frac{L_{st}}{R} = \frac{\psi_m^2}{l/R + \xi R}$$

$$\left(\psi_c^{(110)}/\psi_c^{(111)}\right)^2 \approx 1,25$$

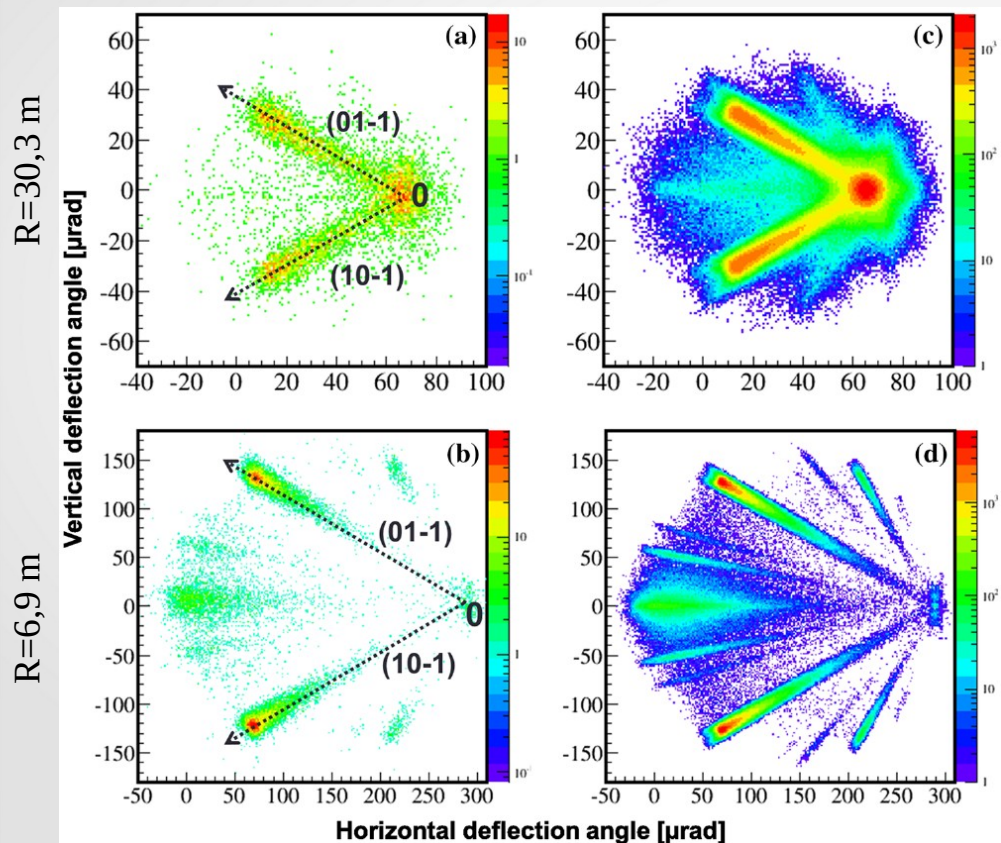


$$(\theta_x - \theta_B)^2 + \theta_y^2 \leq \psi_c^2$$

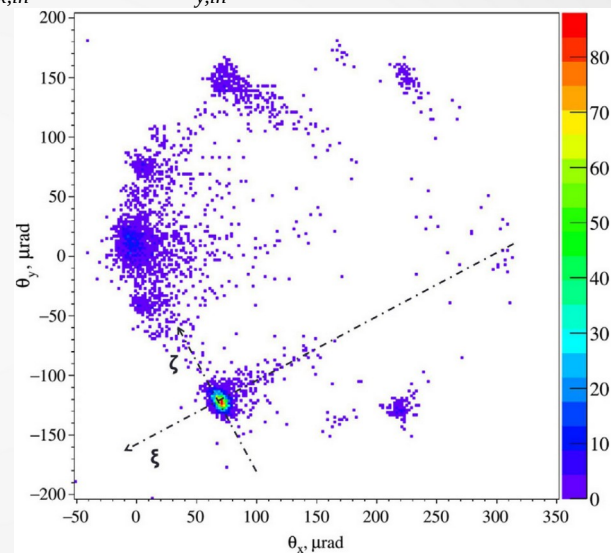
$e^\pm, E=120 \text{ GeV, Si, } L=2 \text{ mm, } \alpha=90 \text{ } \mu\text{rad}$

Changing the shape of the beam

$p, E=400 \text{ GeV}, \text{Si } \langle 111 \rangle, L=2 \text{ mm}$



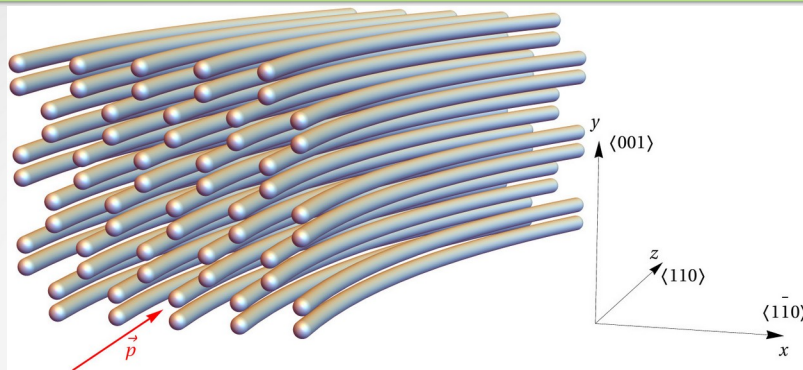
$p, E=400 \text{ GeV}, \text{Si } \langle 111 \rangle, L=2 \text{ mm}, R=6,9 \text{ m},$
 $\theta_{x,in}=-8 \mu\text{rad}, \theta_{y,in}=-4 \mu\text{rad}$



Bandiera L., Mazzolari A., Bagli E. et al. (Kirillin I. V.). Relaxation of axially confined 400 GeV/c protons to planar channeling in a bent crystal. *Eur. Phys. J. C.* 2016. Vol. 76. P. 80 (1–6).
 Bandiera L., Kirillin I. V., Bagli E. et al. Splitting of a high-energy positively-charged particle beam with a bent crystal. *Nucl. Instr. Meth. Phys. Res. B.* 2017. Vol. 402. P. 296–299.

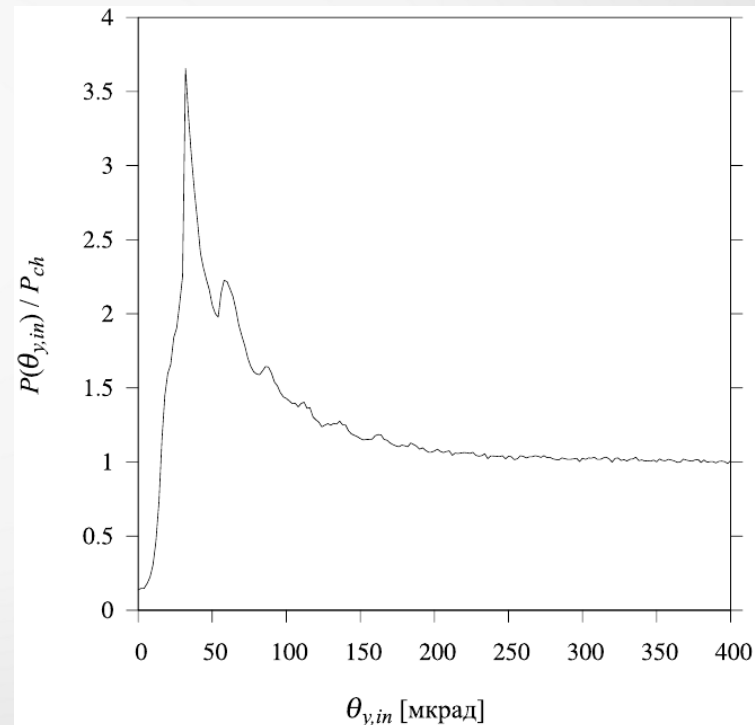
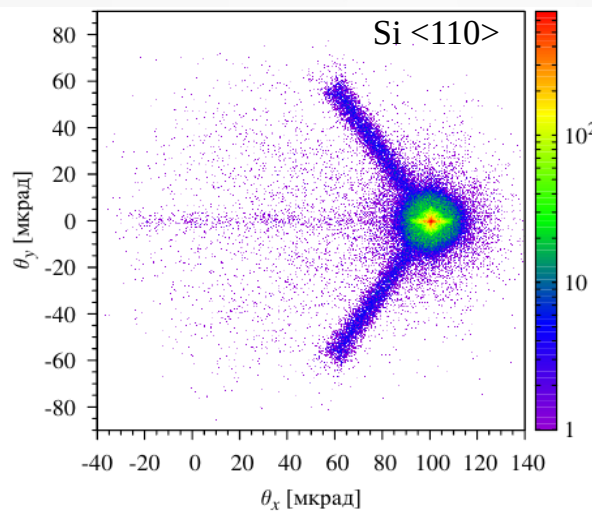
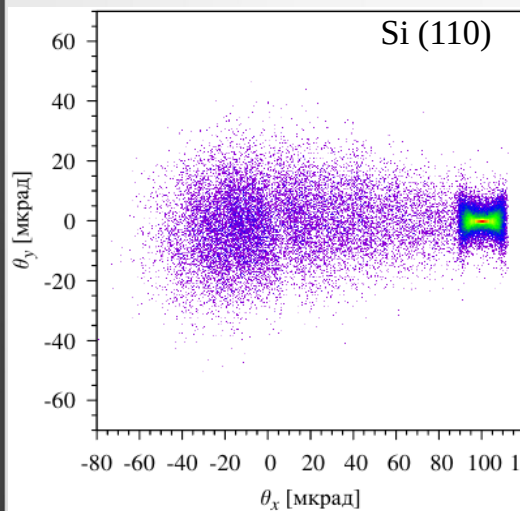
Probability of close collisions

p , $E=270$ GeV,
Si $\langle 110 \rangle$, (110) ,
 $L = 5$ mm,
 $R = 5$ m



$$w_a = \frac{4\pi r_T^2}{a_x a_y} = 4\sqrt{2}\pi r_T^2 / a^2 \approx 3.39 * 10^{-3}$$

$$w_p = \frac{4r_T}{a_x} = 4\sqrt{2}r_T / a \approx 78.12 * 10^{-3}$$



Probability of close collisions

Scandale W., Arduini G., Butcher M. et al. *Phys. Lett. B.* 2016. Vol. 760. P. 826–831.

Scandale W., Andrisani F., Arduini G. et al. *Eur. Phys. J. C.* 2018. Vol. 78, No. 6. P. 505.

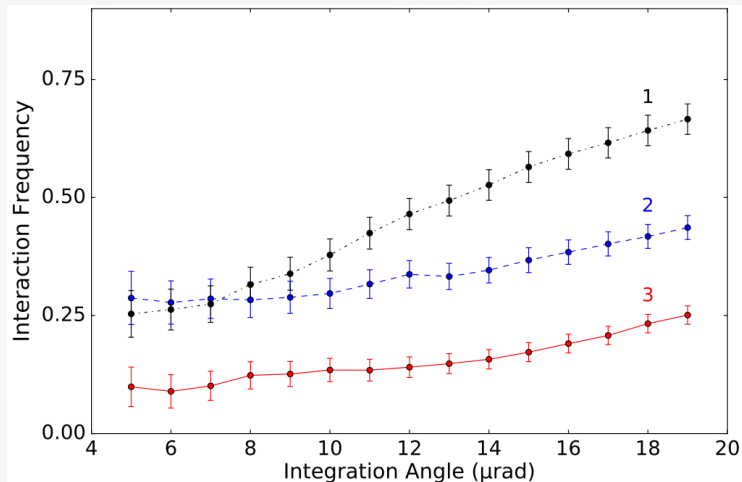
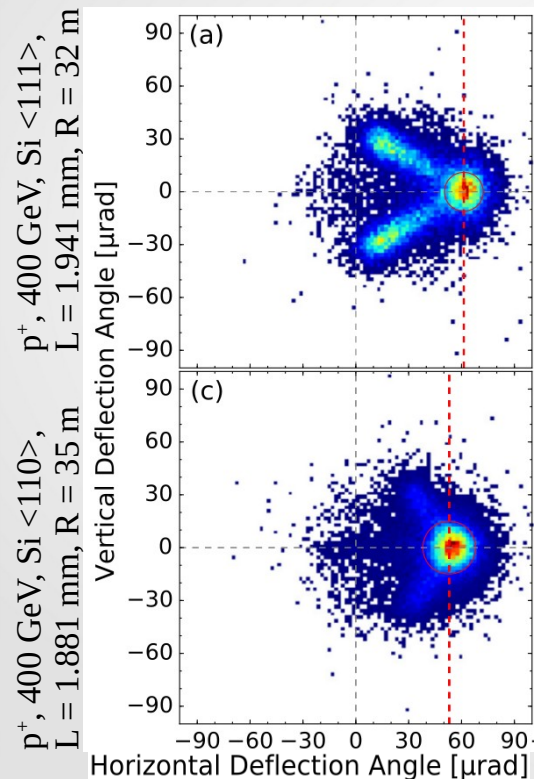
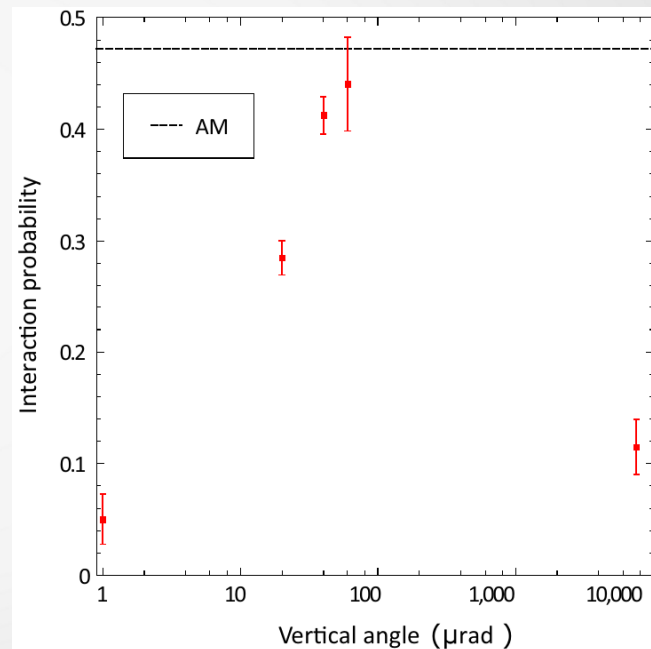
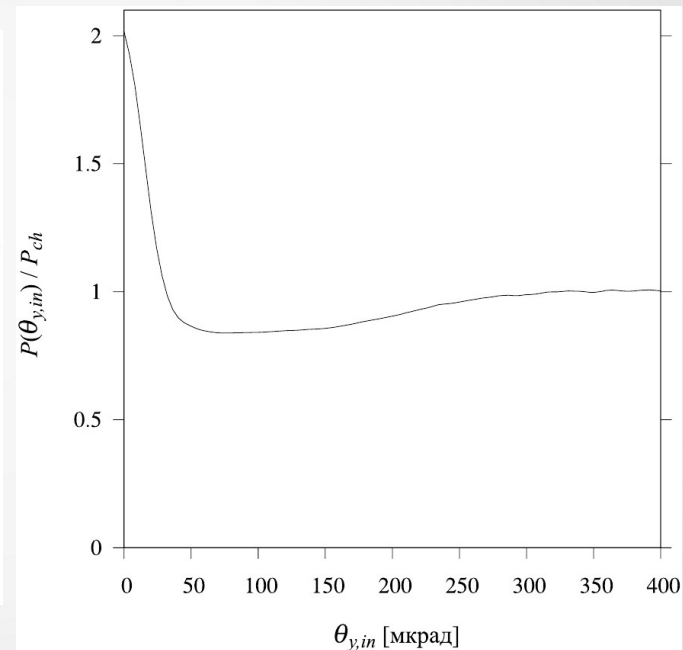
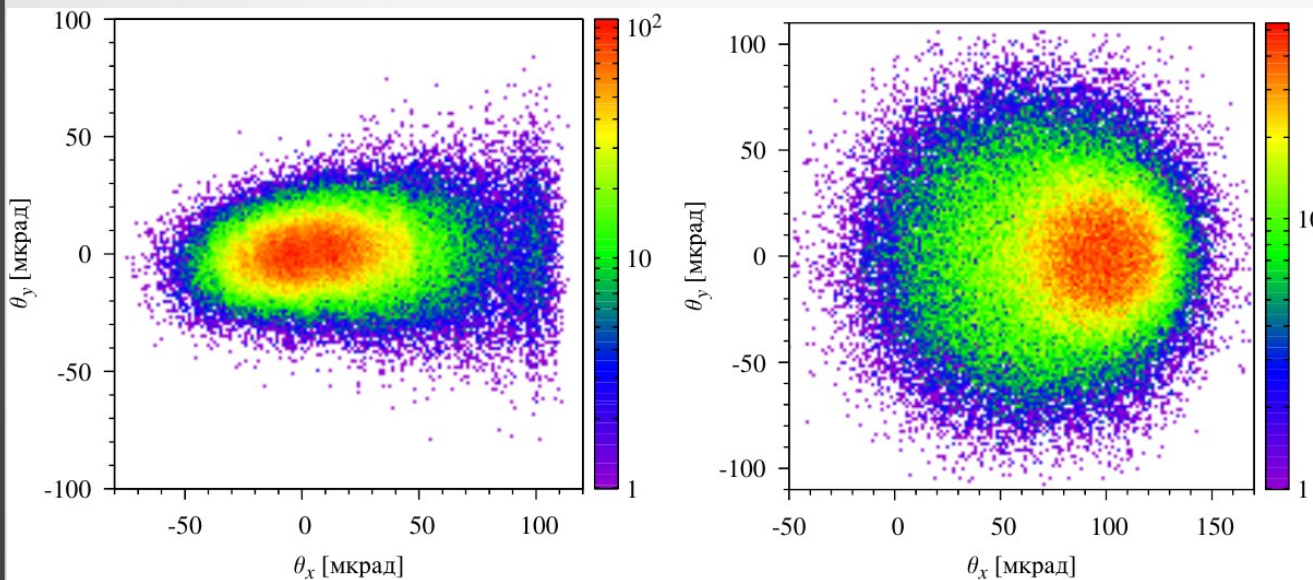


Fig. 5. Measured inelastic nuclear interaction (INI) frequency of 400 GeV/c protons interacting with the $\langle 111 \rangle$ and $\langle 110 \rangle$ crystals as a function of the angular region around the $\langle 110 \rangle$ planar channeling (black dash-dotted line, 1), the $\langle 111 \rangle$ axial channeling (blue dashed line, 2) and $\langle 110 \rangle$ (red continuous line, 3) orientations. The values are normalized to the INI frequencies for the amorphous crystal orientation. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



Probability of close collisions

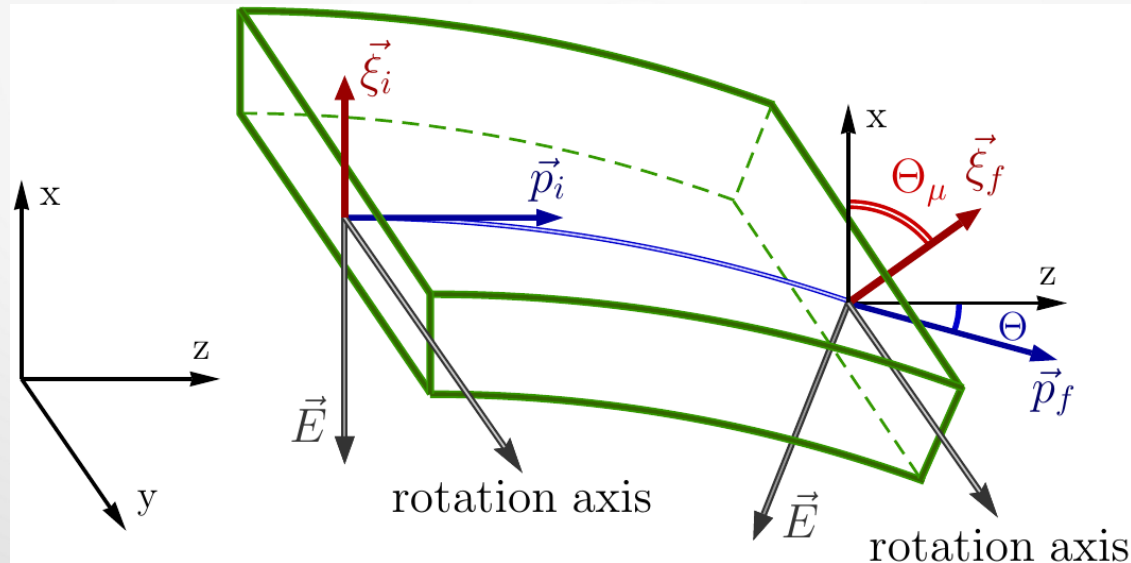
π^- , $E = 270$ ГэВ, Si $\langle 110 \rangle$, $L = 5$ mm, $R = 5$ m



Feasibility of measuring the magnetic dipole moments of the charm baryons at the LHC using bent crystals

Fomin A.S., Korchin A.Yu., Stocchi A. et al. (S.P. Fomin, I.V. Kirillin, N.F. Shul'ga) J. High Energy Phys. 2017. Vol. 2017. № 8. P. 120 (1–26).

$$\Theta_\mu = \gamma \left(\frac{g}{2} - 1 - \frac{g}{2\gamma^2} + \frac{1}{\gamma} \right) \Theta \approx \gamma \left(\frac{g}{2} - 1 \right) \Theta \quad (\text{V.G. Baryshevsky, 1979; V.L. Lyuboshits, 1980})$$



Optimal radius of curvature (stochastic deflection)

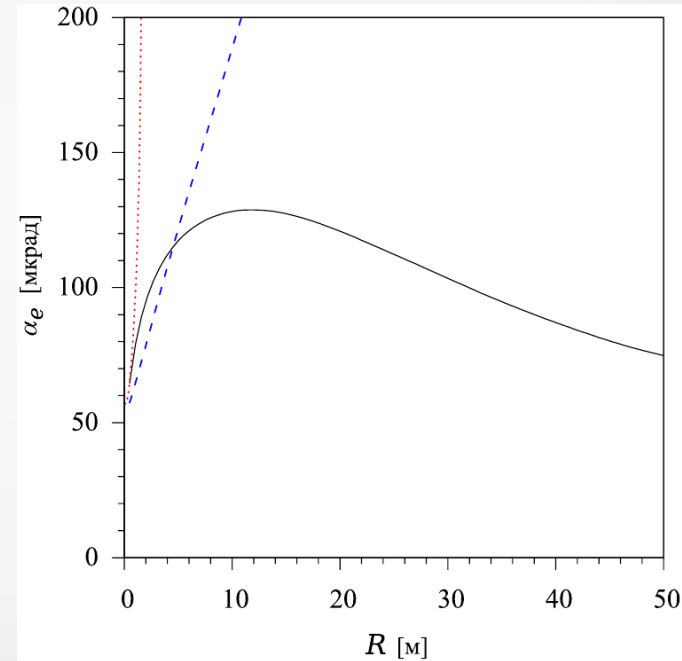
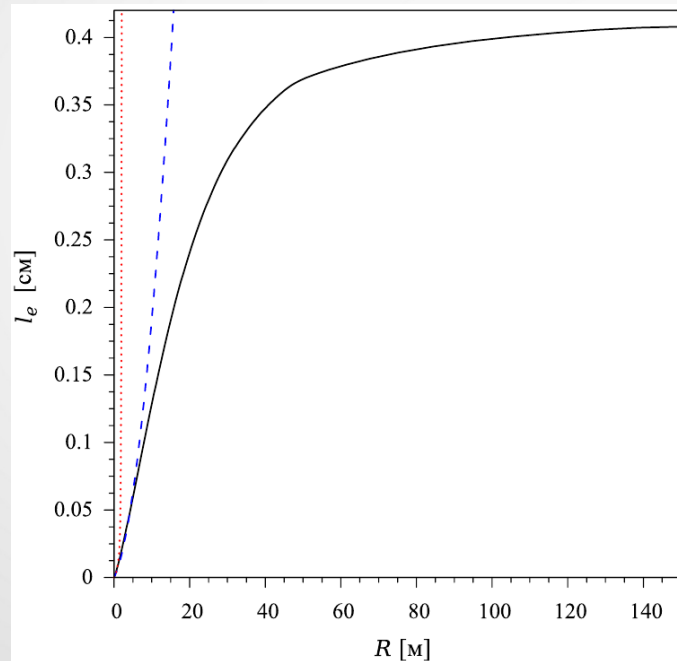
$$\langle \psi^2 \rangle = \frac{lL}{R^2} \leq \psi_c^2$$

$$\overline{\Psi_{inc}^2} = \xi L$$

$$L_{st} = \frac{\psi_m^2}{l/R^2 + \xi}$$

$$\alpha_{st} = \frac{L_{st}}{R} = \frac{\psi_m^2}{l/R + \xi R}$$

π^- , $E=150$ GeV, Si $\langle 110 \rangle$



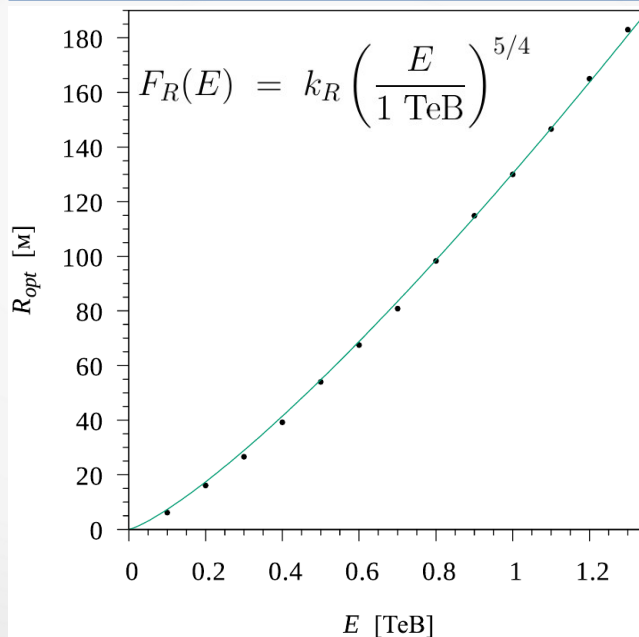
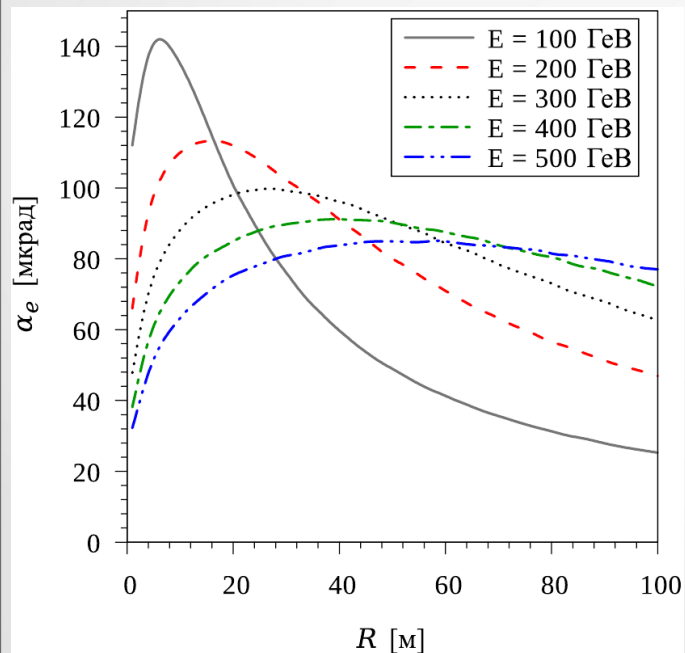
Optimal radius of curvature (stochastic deflection)

$$\overline{\psi_{inc}^2} = \zeta L / E^2 \quad \rightarrow \quad \alpha_{st} = \frac{\psi_m^2}{l/R + \zeta R/E^2} \quad \rightarrow \quad R_{opt} = E \sqrt{l/\zeta}$$

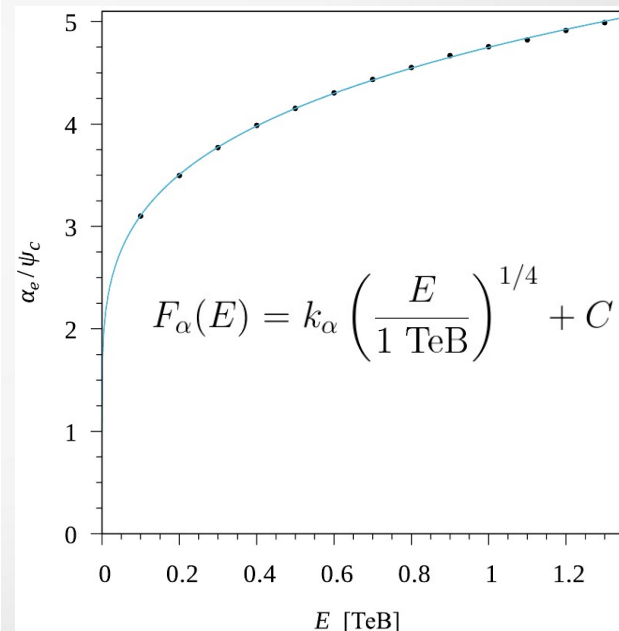
$$l \approx \frac{1}{4\pi n_a} \sqrt{\frac{E}{U_0}} \quad \rightarrow \quad R_{opt} \propto E^{5/4}$$

$$\psi_m \approx 1,5\psi_c \propto E^{-1/2} \quad \rightarrow \quad \max(\alpha_{st}) = \frac{\psi_m^2}{l/R_{opt} + \zeta R_{opt}/E^2} \propto E^{-1/4}$$

π^- , Si <110>



$$k_R \approx 130 \text{ м}$$



$$k_\alpha \approx 3,75 \text{ и } C \approx 1 \quad 16$$

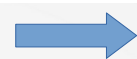
Optimal radius of curvature (planar channeling)

$$\frac{d^2x}{dt^2} = -\frac{c^2}{E} \frac{dU_{\text{eff}}(x)}{dx}$$

$$U_{\text{eff}}(x) = U_p(x) + Ex/R$$

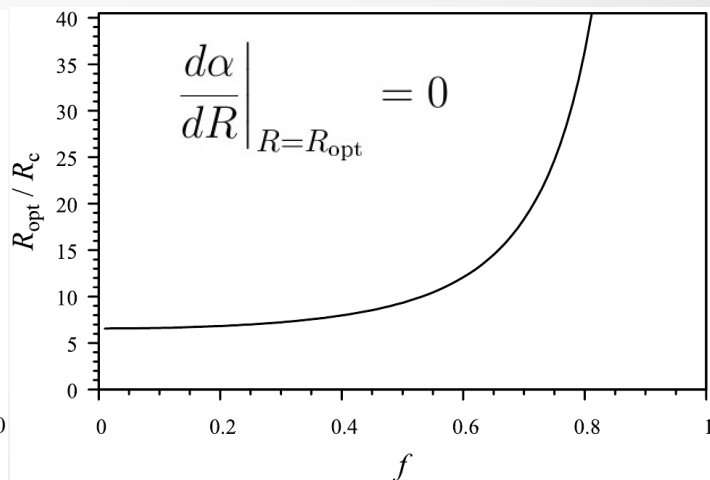
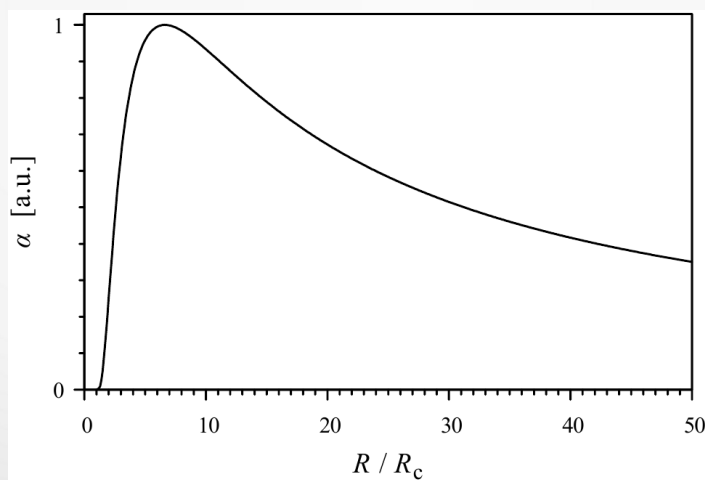
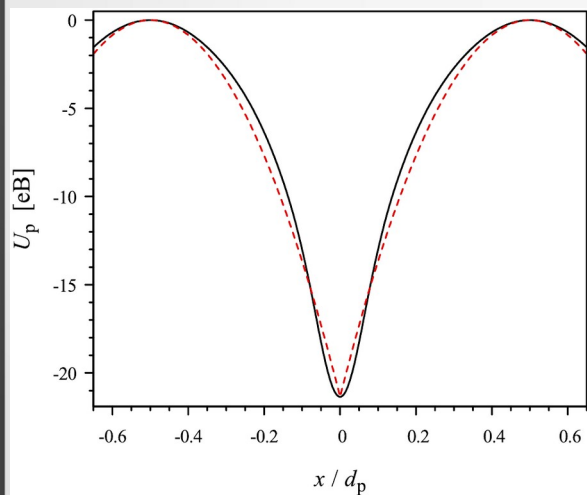
$$U_p(x) = -\frac{U_0}{d_p^2} \left((2x + d_p)^2 H(-x(d_p + x)) + (2x - d_p)^2 H(x(d_p - x)) \right)$$

$$R > R_c$$



$$\frac{x_{\text{pos}} - x_{\text{neg}}}{d_p} = 1 - \sqrt{\frac{R_c}{R}}$$

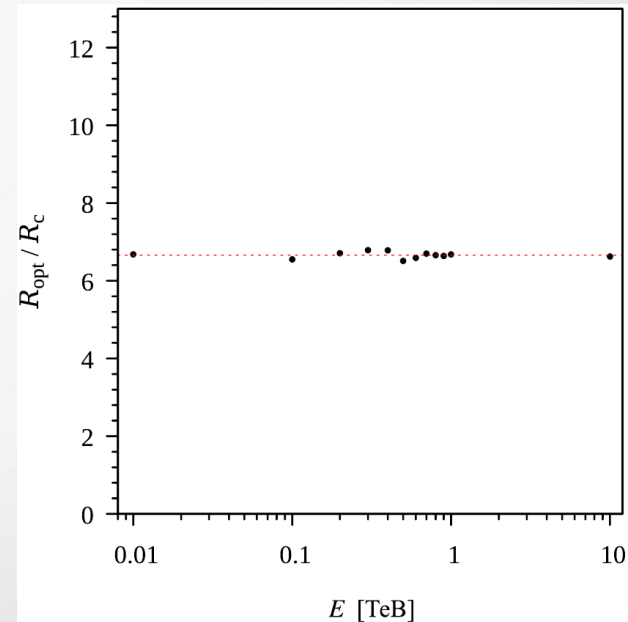
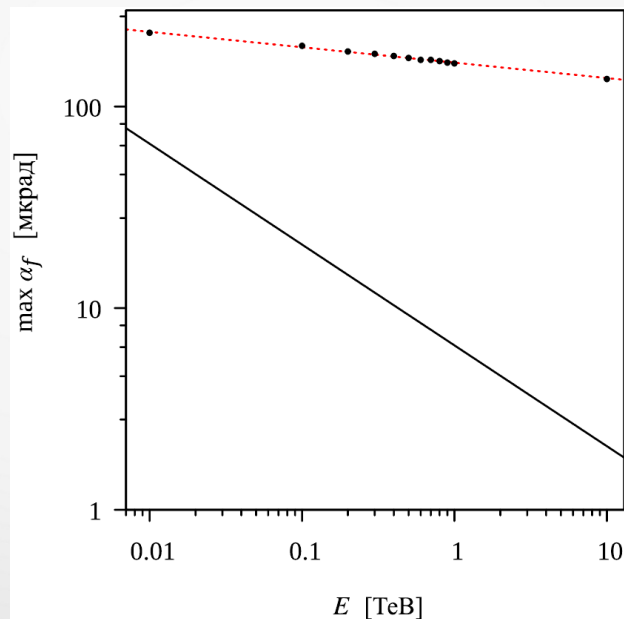
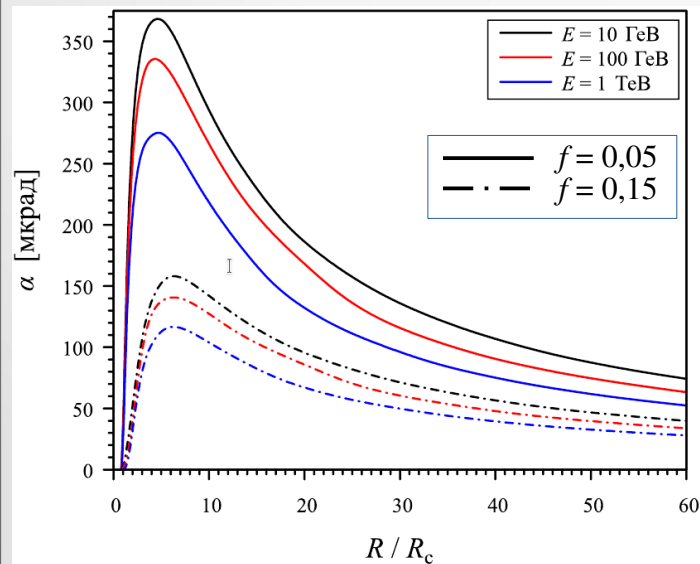
$$\alpha = \frac{l}{R} = \frac{\theta_c^2}{2\xi_p^2 R \left(\text{erf}^{-1} \left(\frac{f}{1 - \sqrt{\frac{R_c}{R}}} \right) \right)^2}$$



Optimal radius of curvature (planar channeling)

$$U_{\text{str}}(\rho) = -\frac{8\pi^2\hbar^2}{m_e d} \sum_{k=1}^4 \frac{\alpha_k}{\beta_k + B} e^{-\frac{4\pi^2\rho^2}{\beta_k + B}} \longrightarrow U_{\text{pl}}(x) = -\frac{4\pi^{\frac{3}{2}}\hbar^2}{m_e d d_s} \sum_{k=1}^4 \frac{\alpha_k}{\sqrt{\beta_k + B}} e^{-\frac{4\pi^2 x^2}{\beta_k + B}}$$

$$U_p(x) = \sum_{n=-\infty}^{\infty} U_{\text{pl}}(x - x_n) \longrightarrow U_p(x) = -\frac{2\pi\hbar^2}{m_e d d_s d_p} \sum_{k=1}^4 \alpha_k \theta_3 \left(\pi \frac{x}{d_p}, e^{-\frac{\beta_k + B}{4d_p^2}} \right)$$



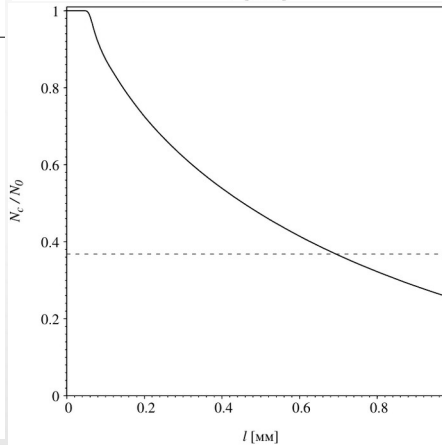
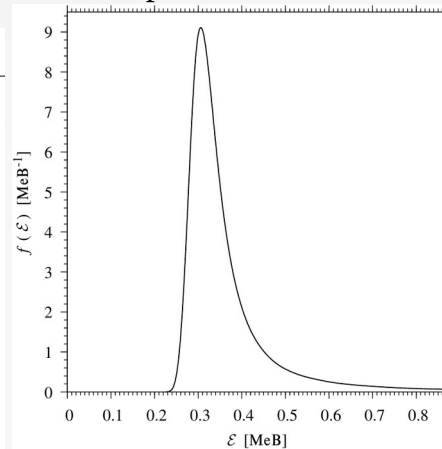
Ionization loss in a crystal

π^- , $E=150$ ГэВ, Si, $L=1$ мм

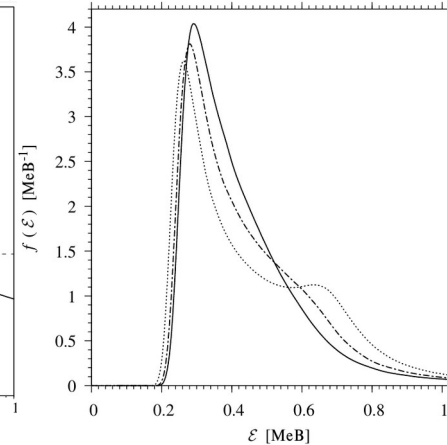
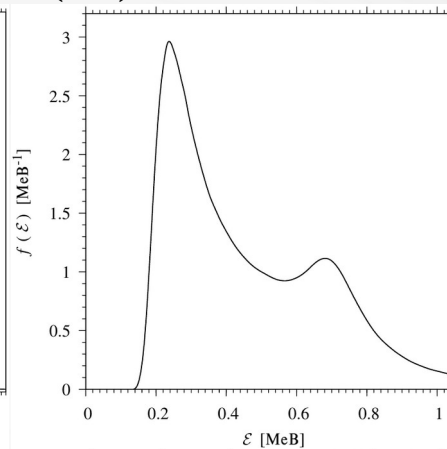
$$l_d = \xi E$$

Площина	Частинки	E [ГэВ]	ξ [мкм/ГэВ]	Джерело
(110)	e^-		17,8	[353]
(110)	e^-	0,855	21,1	[107]
(110)	e^-	0,855	48,0	[354]
(110)	e^-	0,855	9,7	[355]
(110)	e^-	1,2	24,2	[356]
(110)	π^-	150	6,2	[357]
(111)	e^-		23,6	[353]
(111)	e^-	0,855	23,7	[358]
(111)	e^-	0,855	15,9	[355]
(111)	e^-	3,35–14	15,3	[187]
(111)	e^-	0,5–100	27	[359]
(111)	e^-	50	6,6	[360]

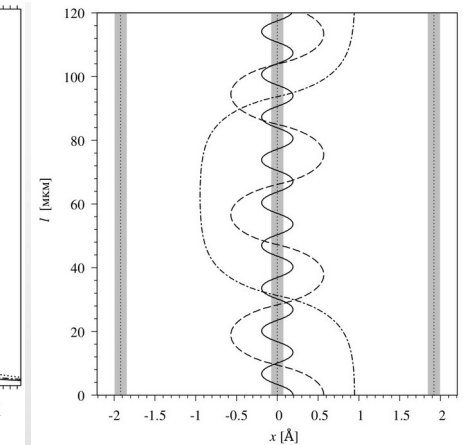
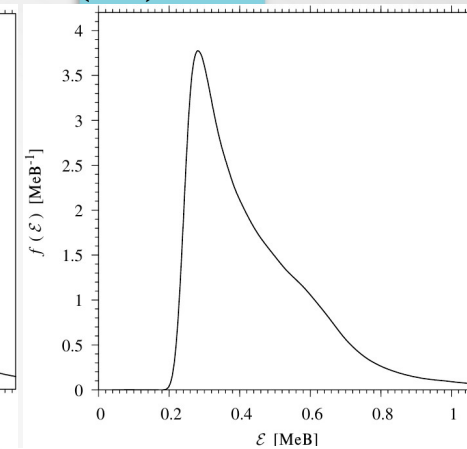
amorphous orientation



(110) without incoh. scatt.

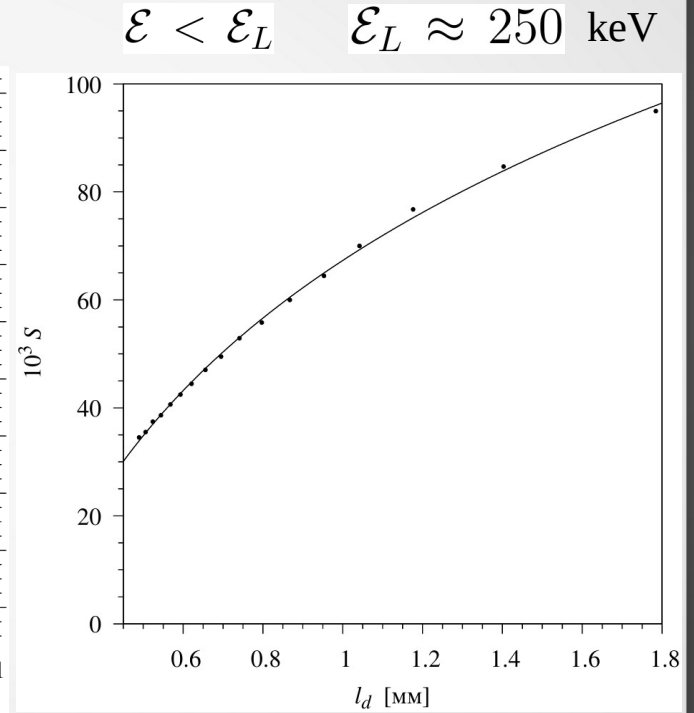
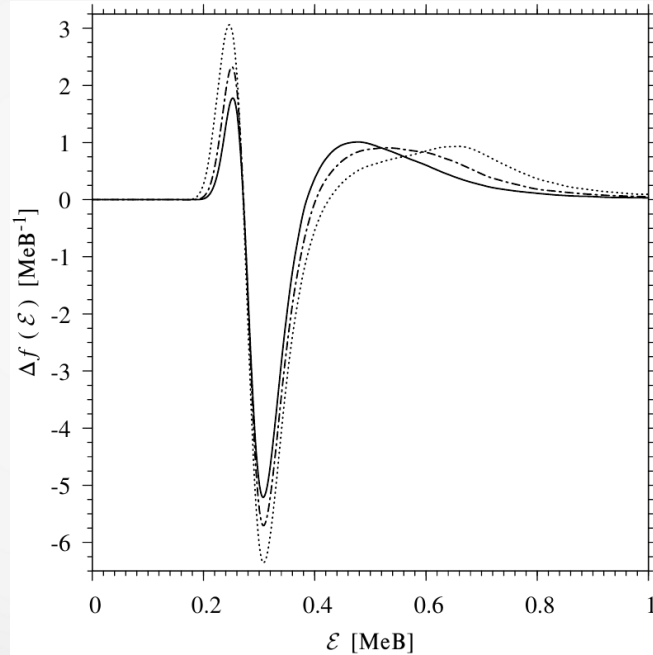
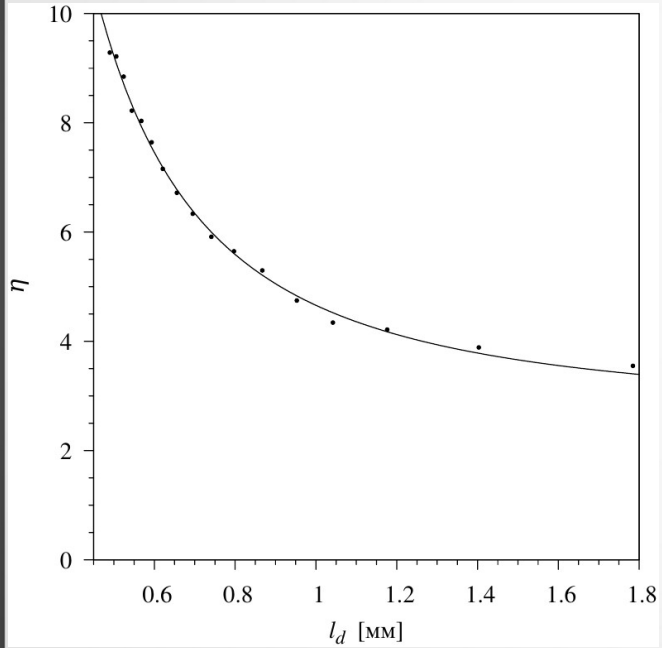


(110) with incoh. scatt.



Ionization loss in a crystal

$$\eta = f(\mathcal{E}_{\max})/f(\mathcal{E}_R)$$





Дякую за увагу!